

## INTRODUCTION

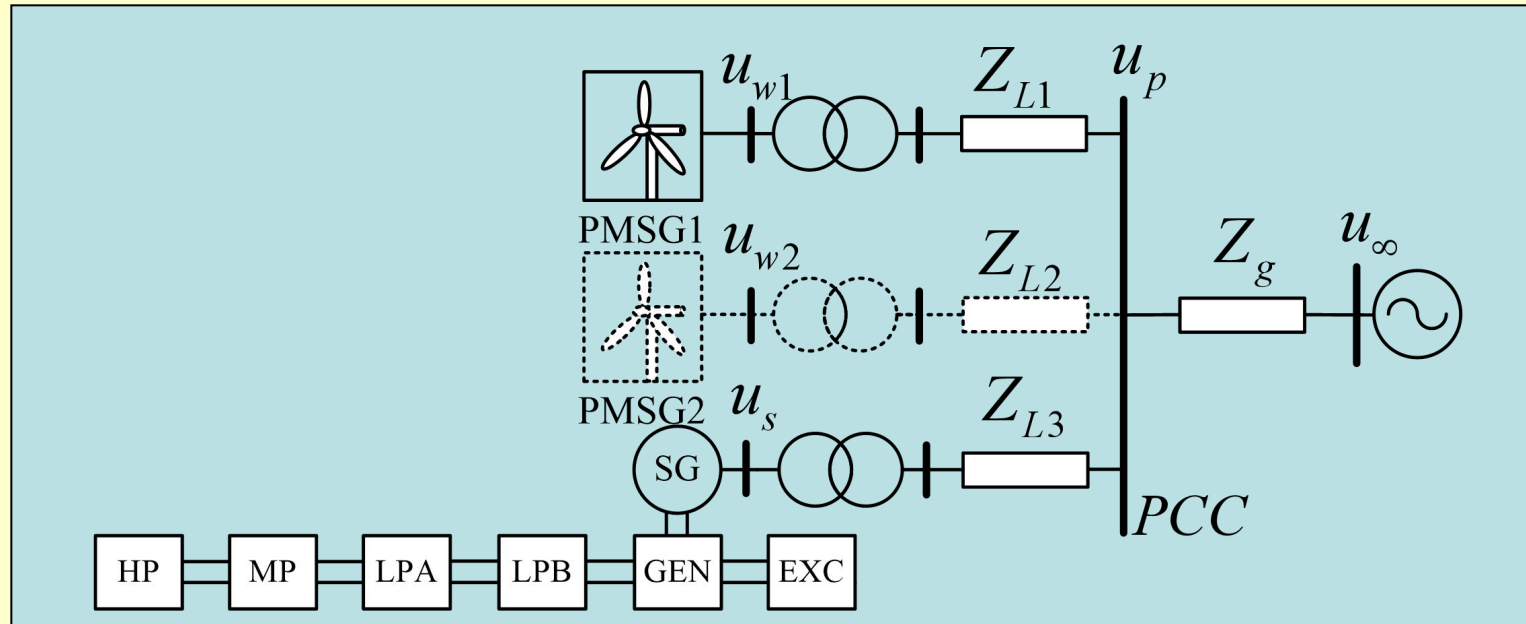


Fig.1 The studied system

The PMSG wind farms connected to the weak grid may induce the subsynchronous torsional oscillations (SSTOs). Different from the traditional subsynchronous resonance, there is no series compensated lines in the power grid and the power electronic equipment is the inducement of oscillation.

This paper studies the mechanism of the SSTOs induced by PLL-dominated mode and influencing factors of torsional mode stability.

## THE SMALL-SIGNAL MODEL OF STUDIED SYSTEM

$$\begin{cases} \Delta \dot{\mathbf{x}}_s = \mathbf{A}_s \Delta \mathbf{x}_s + \mathbf{B}_s \Delta \mathbf{u}_s \\ \Delta \mathbf{i}_s = \mathbf{C}_s \Delta \mathbf{x}_s \end{cases} \quad (1) \quad \begin{cases} \Delta \dot{\mathbf{x}}_w = \mathbf{A}_w \Delta \mathbf{x}_w + \mathbf{B}_w \Delta \mathbf{u}_w \\ \Delta \mathbf{i}_w = \mathbf{C}_w \Delta \mathbf{x}_w \end{cases} \quad (2) \quad \begin{cases} \Delta u_{ix} = L_{ij} \frac{d\Delta i_{ijx}}{dt} - L_{ij} \Delta i_{ijy} + R_{ij} \Delta i_{ijx} + \Delta u_{jx} \\ \Delta u_{iy} = L_{ij} \frac{d\Delta i_{ijy}}{dt} + L_{ij} \Delta i_{ijx} + R_{ij} \Delta i_{ijy} + \Delta u_{jy} \end{cases} \quad (3)$$

The small-signal model of SG      The small-signal model of PMSG      The small-signal model of transmission line

$$\Delta \dot{\mathbf{x}} = \mathbf{A}_{sys} \Delta \mathbf{x}$$

The IEEE first benchmark model is adopted and only the grid-side controller of PMSG is considered. The  $\mathbf{A}_{sys}$  is a  $26 \times 26$  matrix.

## THE MECHANISM AND INFLUENCING FACTORS of SSTOs

### The single PMSG and single SG system

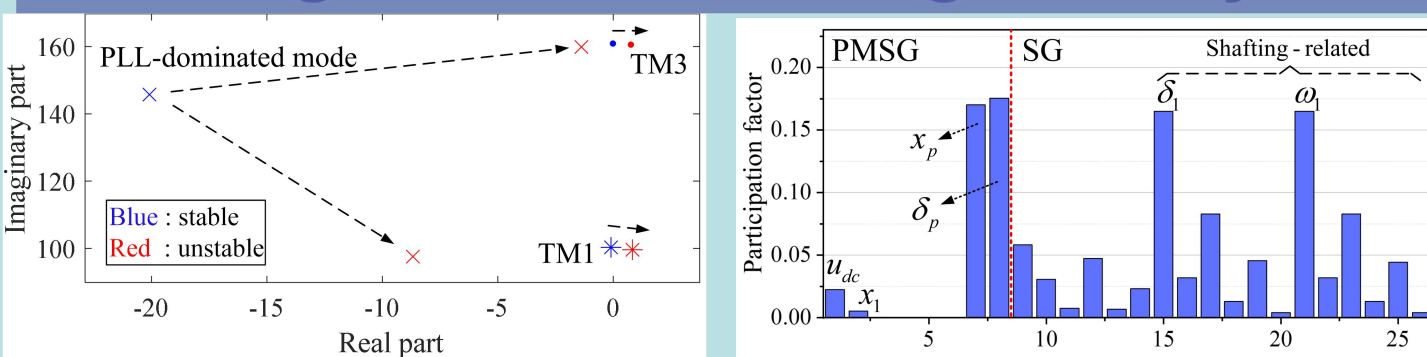


Fig.2 trajectory diagram of eigenvalues (Cross sign: PLL-dominated mode; Point: TM3; Asterisk: TM1)

Fig.3 Participation factors of each state variable in unstable TM3

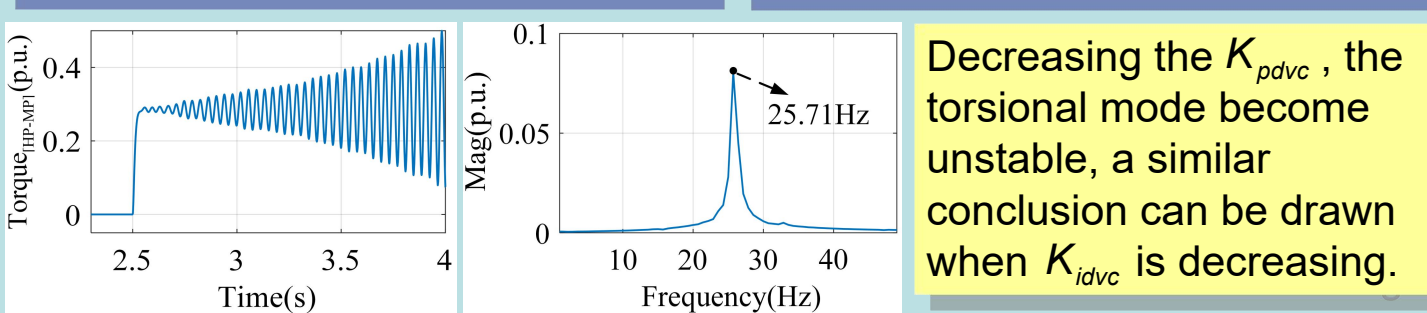


Fig.4 The torque between HP and MP, and its FFT analysis

Decreasing the  $K_{pdvc}$ , the torsional mode become unstable, a similar conclusion can be drawn when  $K_{idvc}$  is decreasing.

Fig.5 The trajectories of PLL-dominated mode, DVC-dominated mode and TM3

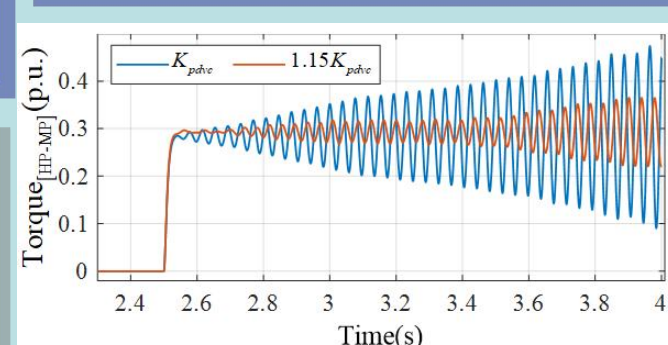


Fig.6 The HP-MP torque under different  $K_{pdvc}$

### The Multi-PMSGs and single SG system

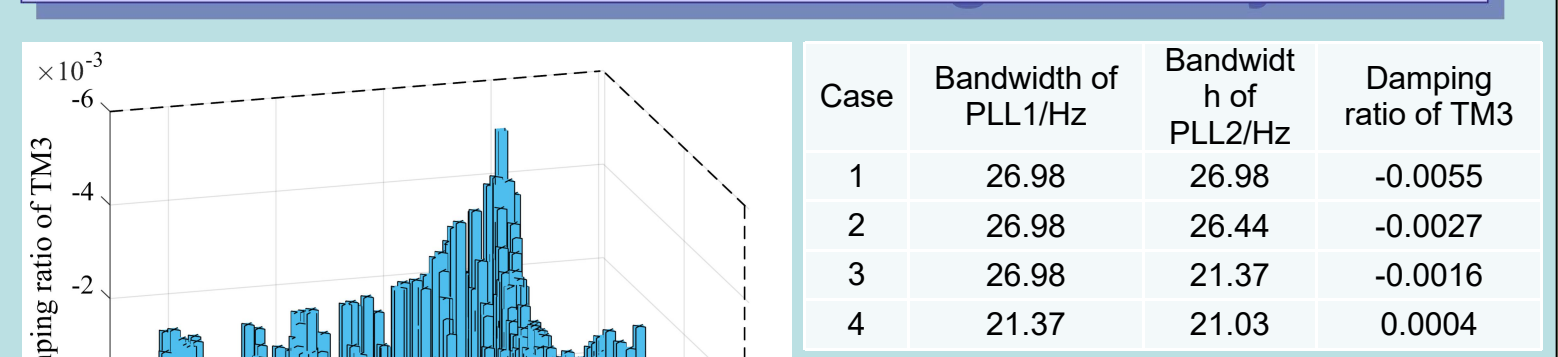


Fig.7 The damping ratio of TM3 when the Monte Carlo method is used to randomly generate PLL parameters

Case	Bandwidth of PLL1/Hz	Bandwidth of PLL2/Hz	Damping ratio of TM3
1	26.98	26.98	-0.0055
2	26.98	26.44	-0.0027
3	26.98	21.37	-0.0016
4	21.37	21.03	0.0004

Table.1 PLL parameters of PMSGs under different cases

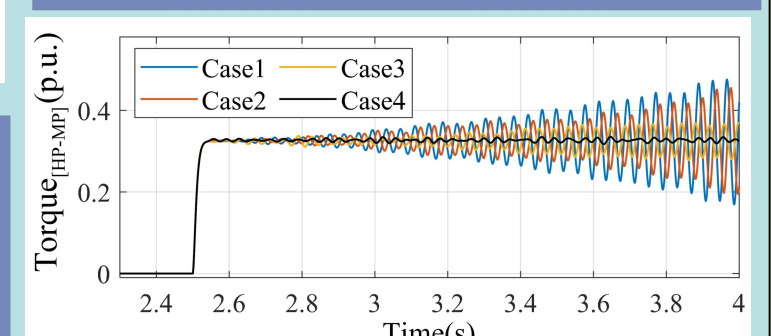


Fig.8 The HP-MP torque under different cases

Mechanism explanation: Fig. 2 shows that weakening the damping of PLL-dominated mode, make it approaches the imaginary axis, when its frequency is close to the frequency of the torsional modes, it will cause the torsional mode to enter the right side of the complex plane, the SSTOs will be induced. The time domain simulation in Fig.4 reproduces the SSTOs phenomenon.

## Summary

When the PLL-dominated mode "approaches" to the torsional mode, the interaction between the PMSG and the SG will cause the torsional mode to enter the right side of the complex plane, and the SSTOs occur. At the same time, DVC parameters have a non-negligible influence on torsional mode stability.

In a multi-PMSGs grid-connected system, when the bandwidth of each PLL is close to the frequency of torsional mode, the risk of SSTOs in the system is high.